

Learning from Smart Lagrangian particles in turbulent flows: one-way and two-way coupling  
(a journey in Mare Incognitum)

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# NAVIER-STOKES 3D $\leftrightarrow$ 2D

(NASA - Space Flight Center Scientific Visualization Studio)



2D

(Vortices within vortices - APS Gallery of Fluid Motions)

Entry #: 84174

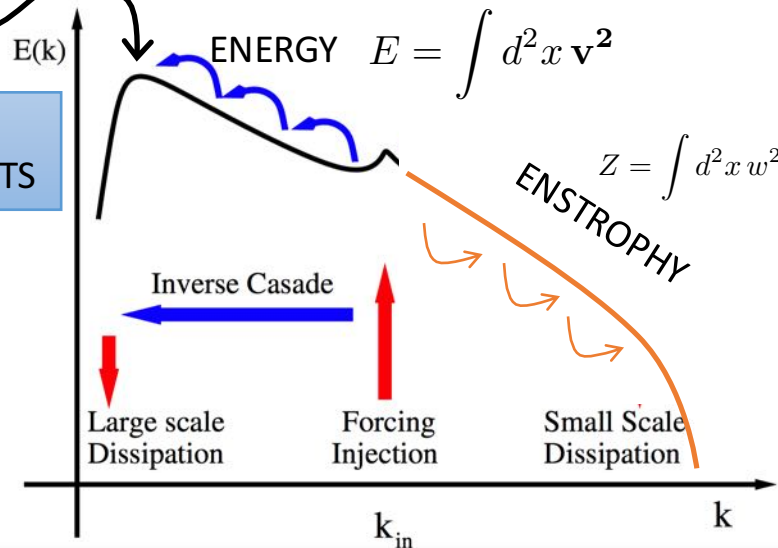
Vortices within vortices:  
hierarchical nature of vortex tubes in turbulence

Kai Bürger<sup>1</sup>, Marc Treib<sup>1</sup>, Rüdiger Westermann<sup>1</sup>,  
Suzanne Werner<sup>2</sup>, Cristian C Lalescu<sup>3</sup>,  
Alexander Szalay<sup>2</sup>, Charles Meneveau<sup>4</sup>, Gregory L Eyink<sup>2,3,4</sup>

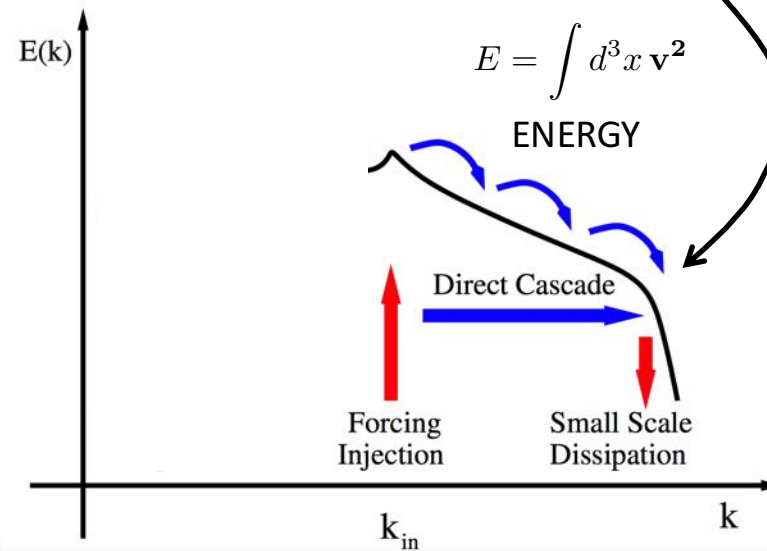
<sup>1</sup> Informatik 15 (Computer Graphik & Visualisierung), Technische Universität München  
<sup>2</sup> Department of Physics & Astronomy, The Johns Hopkins University  
<sup>3</sup> Department of Applied Mathematics & Statistics, The Johns Hopkins University  
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3D

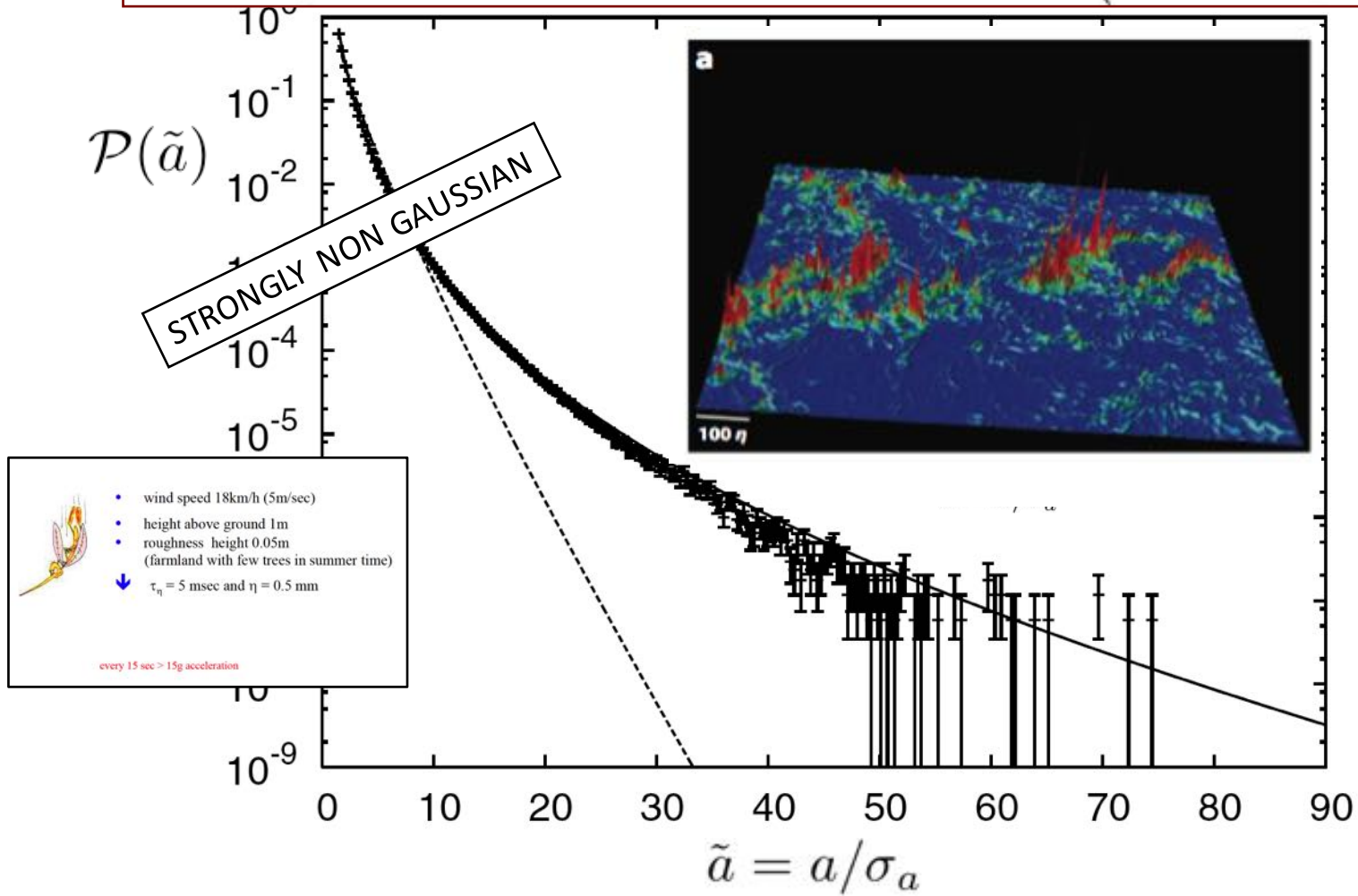
LARGE-SCALE  
EXTREME-EVENTS



SMALL-SCALE  
EXTREME-EVENTS



$$\mathcal{P}(a) \sim \int_{h \in I} dh a^{\frac{h-5+D(h)}{3}} \nu^{\frac{7-2h-2D(h)}{3}} L_0^{D(h)+h-3} \sigma_v^{-1} \times \exp\left(-\frac{a^{\frac{2(1+h)}{3}} \nu^{\frac{2(1-2h)}{3}} L_0^{2h}}{2\sigma_v^2}\right)$$



L. B., G. Boffetta, A. Celani, B. Devenish, A. Lanotte and F. Toschi *Physical Review Letters* **93**, 064502, 2004

LARGE-SCALE  
EXTREME-EVENTS



Starry night (V. van Gogh, 1889)

Road with Cypress and Star  
(V. van Gogh, 1890)



**Turbulent luminance in impassioned van Gogh paintings**  
[J.L. Aragón](#), [Gerardo G. Naumis](#), [M. Bai](#), [M. Torres](#), [P.K. Maini](#)

[arXiv:physics/0606246](#) [physics.flu-dyn]

[journal of Mathematical Imaging and Vision](#)

March 2008, Volume 30, [Issue 3](#), pp 275–283 |

Turbulent Luminance in Impassioned van Gogh Paintings

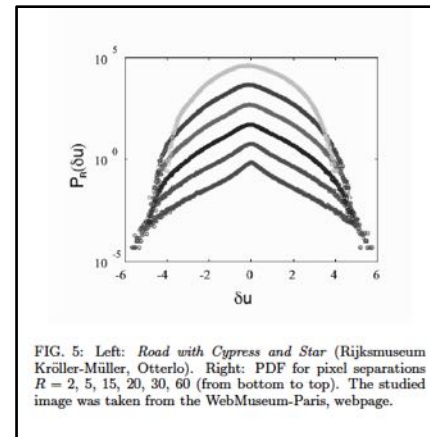
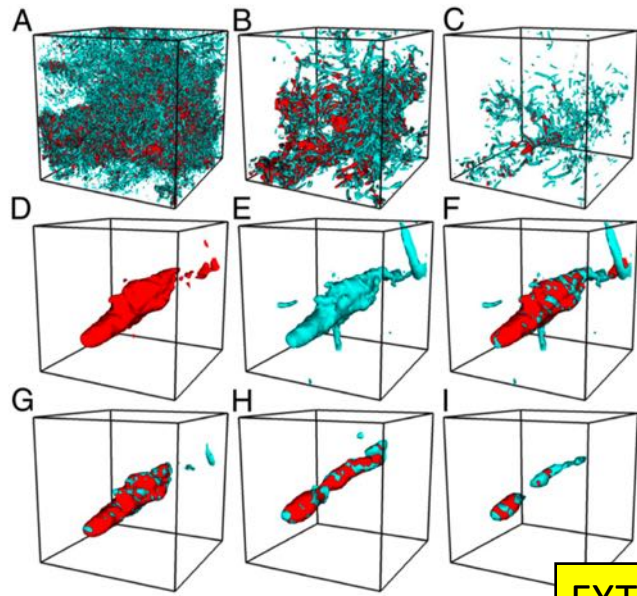
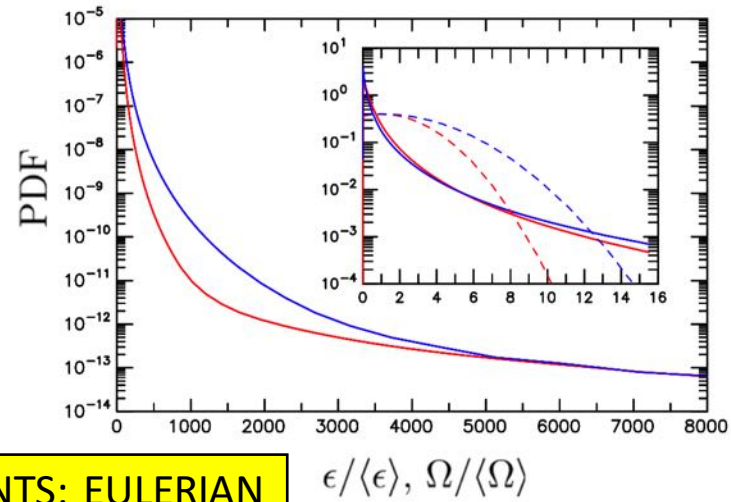


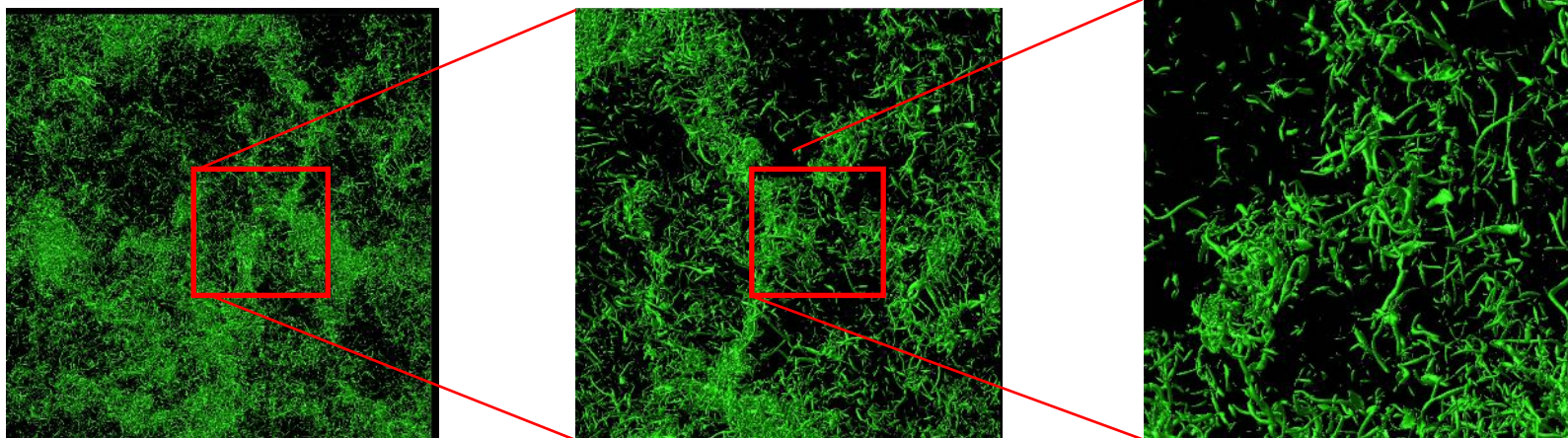
FIG. 5: Left: *Road with Cypress and Star* (Rijksmuseum Kröller-Müller, Otterlo). Right: PDF for pixel separations  $R = 2, 5, 15, 20, 30, 60$  (from bottom to top). The studied image was taken from the WebMuseum-Paris, webpage.



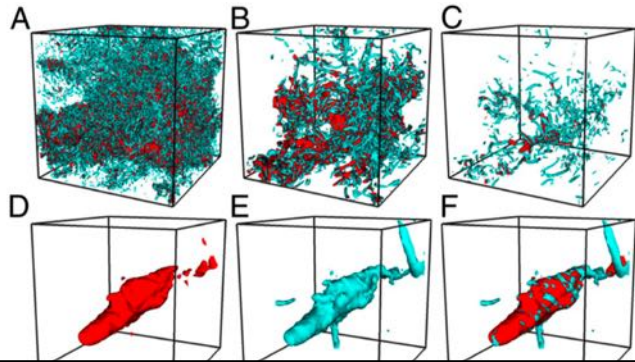
Extreme events in computational turbulence. P. K. Yeung , X. M. Zhai and K.R. Sreenivasan. PNAS 112(41) 12633 (2015)



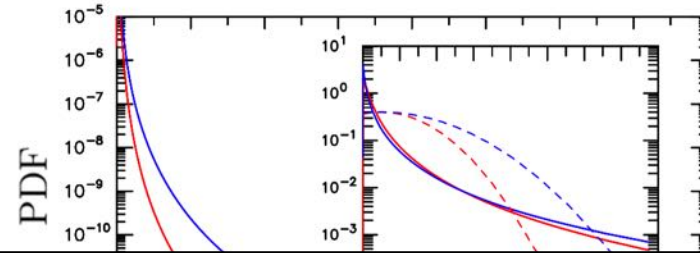
EXTREME EVENTS: EULERIAN



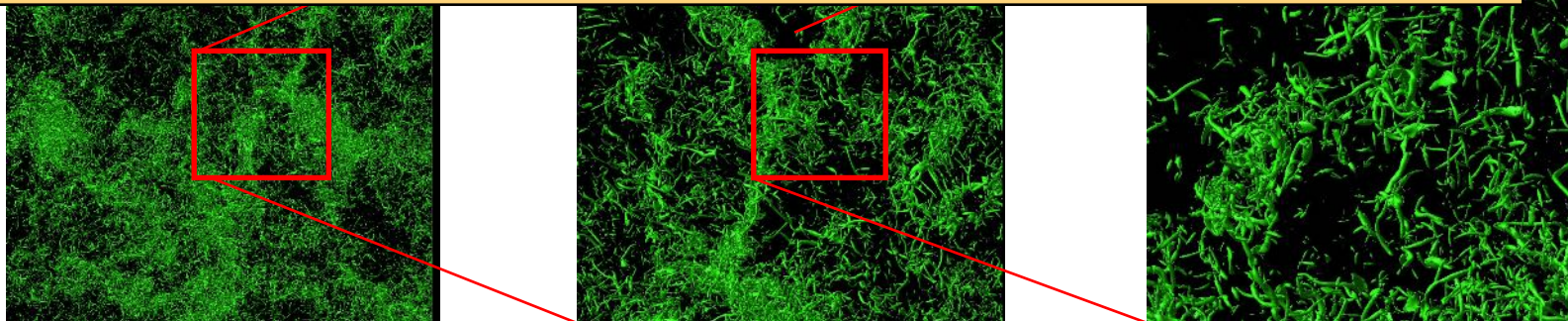
Watanabe and Gotoh, Phys. Fluids 19, 121701 (2007)



Extreme events in computational turbulence. P. K. Yeung , X. M. Zhai and K.R. Sreenivasan. PNAS 112(41) 12633 (2015)

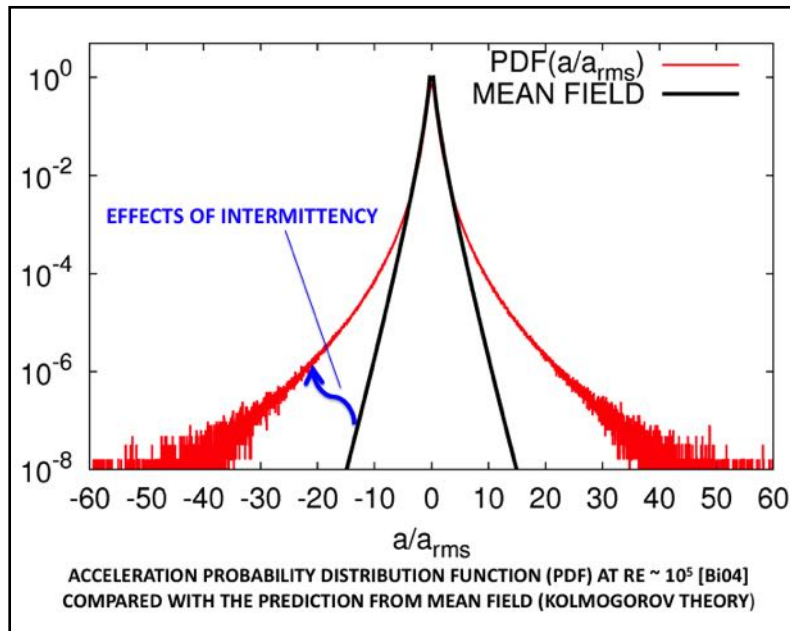
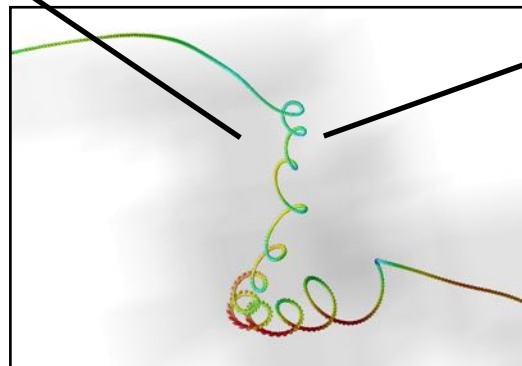
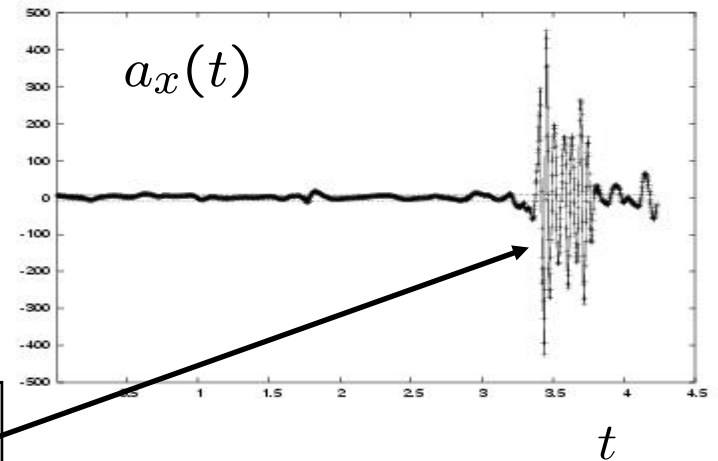
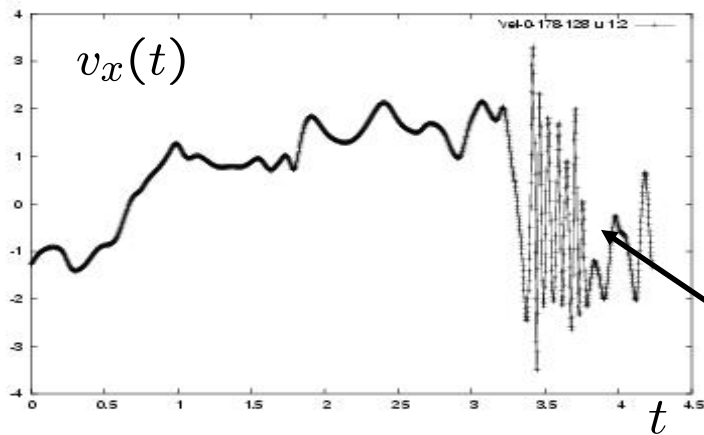


1. IS IT POSSIBLE TO PREFERENTIALLY TRACK INTENSE (LARGE- OR SMALL-SCALE) STRUCTURES?
2. CAN WE INVENT IN-SILICO EXPERIMENTS TO ENGINEER A (LAGRANGIAN) WAY TO CONTROL/STUDY TURBULENCE?
3. CAN WE IDENTIFY THE KEY DEGREES-OF-FREEDOM TO RECONSTRUCT THE FLOW (KEY FLOW STRUCTURES)?
4. ARE THERE REYNOLDS-INDEPENDENT TURBULENT FINGERPRINTS? IF YES: IS IT BETTER TO WORK AT LOW REYNOLDS AND HIGH STATISTICS OR VICEVERSA?

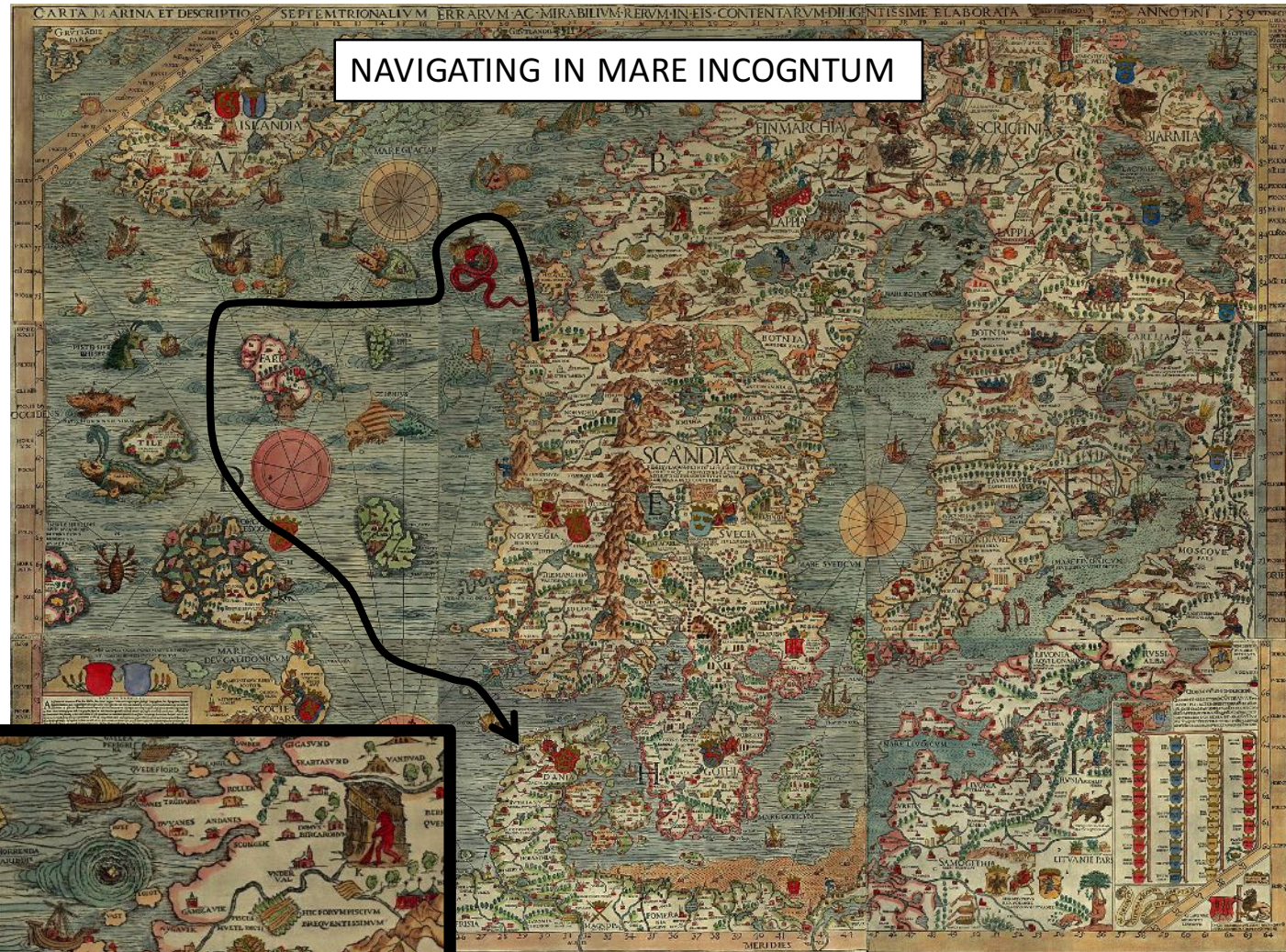


Watanabe and Gotoh, Phys. Fluids 19, 121701 (2007)

## EXTREME EVENTS: LAGRANGIAN



- L.B., G Boffetta, A Celani, A Lanotte, F Toschi. Particle trapping in three-dimensional fully developed turbulence *Physics of Fluids* 17 (2), 021701 (2005)
- La Porta, G.A. Voth, A.M. Crawford, J. Alexander et al. Fluid particle accelerations in fully developed turbulence. *Nature*, 409(6823), 1017 (2001)
- N. Mordant, P. Metz, O. Michel and J.F. Pinton. Measurement of Lagrangian velocity in fully developed turbulence. *Phys. Rev. Lett.* 87(21), 214501 (2001)
- F. Toschi and E. Bodenschatz. Lagrangian Properties of Particles in Turbulence. *Annu. Rev. Fluid Mech.* 41, 375 (2009)

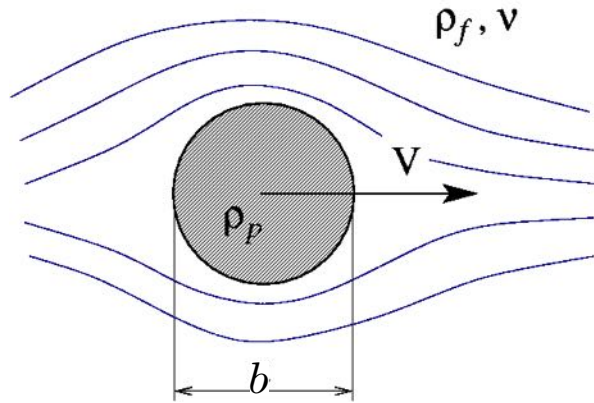


NAVIGATING IN MARE INCOGNITUM

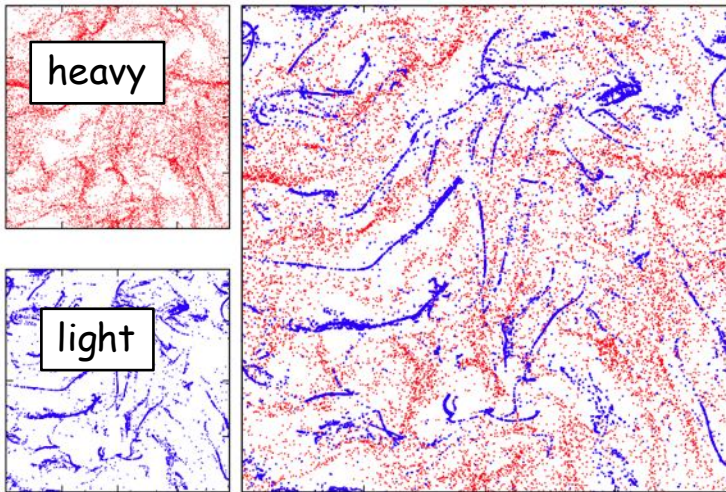
*Carta Marina et descriptio septentrionalium terrarum ac mirabilium rerum in eis contentarum, diligentissime elaborata anno 1539 Veneciis. Oloa Magno*



## INERTIAL PARTICLES IN COMPLEX FLOWS



$$\begin{cases} \partial_t \mathbf{v} + \mathbf{v} \cdot \partial_{\mathbf{x}} \mathbf{v} + \partial_{\mathbf{x}} P = \nu \Delta \mathbf{v} \\ \dot{\mathbf{X}}_i = \mathbf{U}_i \\ \dot{\mathbf{U}}_i = -\frac{\mathbf{U}_i - \mathbf{v}}{\tau} + \beta D_t \mathbf{v} - g(1 - \beta) \hat{\mathbf{z}} \end{cases}$$



$$\beta = \frac{3\rho_f}{\rho_f + 2\rho_p}$$

$$\tau = \frac{\bar{b}^2}{3\nu\beta}$$

$\beta < 1$  heavy particles  
 $\beta > 1$  light particles

Drag: **Stokes Time**

### Preferential concentration

Naive light(heavy) particles accumulate  
 inside(outside) highly vortical regions

## **OLD QUESTIONS:**

1. IS IT POSSIBLE TO PREFERENTIALLY TRACK INTENSE (LARGE- OR SMALL-SCALE) STRUCTURES?
2. CAN WE INVENT IN-SILICO EXPERIMENTS TO ENGINEER A (LAGRANGIAN) WAY TO CONTROL/STUDY TURBULENCE?
3. CAN WE IDENTIFY THE KEY DEGREES-OF-FREEDOM TO RECONSTRUCT THE FLOW (KEY FLOW STRUCTURES)?
4. ARE THERE REYNOLDS-INDEPENDENT TURBULENT FINGERPRINTS? IF YES: IS IT BETTER TO WORK AT LOW REYNOLDS AND HIGH STATISTICS OR VICEVERSA?

## **NEW TOOLS:**

1. **SMART LAGRANGIAN PROBES (ONE-WAY COUPLING):** REINFORCEMENT LEARNING TO TRACK PREFERENTIAL VORTICITY STRUCTURES (OR STRAIN, QUADRANTS, HAIRPINS, THERMAL PLUMES...)
2. **SMART LAGRANGIAN PROBES (TWO-WAY COUPLING):** AD-HOC FEEDBACK ON THE FLOW STRUCTURES TO CONTROL TURBULENCE
3. **NUDGING:** AN EQUATION-INFORMED TOOL TO ASSIMILATE AND RECONSTRUCT TURBULENCE DATA
4. **HYBRID-MONTE-CARLO** FOR MARTIN-SIGGIA-ROSE STOCHASTIC PDES: A TOOL TO PREFERENTIALLY FOCUS ON INTENSE-AND-RARE FLUCTUATIONS (INSTANTONS) AT SMALL REYNOLDS